

## Measures of central tendency

- Used for interval or ordinal data
- “average” or “typical” value
- 3 averages: arithmetic mean, median, mode
- Sometimes equal, sometimes not

## Arithmetic mean

- Assume 10 students have the following academic year earnings

|          |          |
|----------|----------|
| \$7,000  | \$4,000  |
| \$8,000  | \$16,000 |
| \$4,000  | \$7,000  |
| \$25,000 | \$8,000  |
| \$15,000 | \$7,000  |

Arithmetic mean:  
ungrouped data

$$\bar{Y} = \frac{\sum Y}{n}$$

Arithmetic mean:  
ungrouped data

$$= \frac{101,000}{10} = \$10,100$$

Arithmetic mean:  
grouped data

$$\bar{Y} = \frac{\sum fY}{n}$$

Where  $f = \#$  in group

Arithmetic mean:  
grouped data

| <u>Values</u> | <u>Frequency</u> |  |
|---------------|------------------|--|
| 4,000 x       | 2                |  |
| 7,000 x       | 3                |  |
| 8,000 x       | 2                |  |
| 15,000 x      | 1                |  |
| 16,000 x      | 1                |  |
| 25,000 x      | 1                |  |
|               | 10               |  |

## Arithmetic mean: grouped data

| Values   | Frequency | Value x frequency     |
|----------|-----------|-----------------------|
| 4,000 x  | 2         | 8,000                 |
| 7,000 x  | 3         | 21,000                |
| 8,000 x  | 2         | 16,000                |
| 15,000 x | 1         | 15,000                |
| 16,000 x | 1         | 16,000                |
| 25,000 x | 1         | 25,000                |
|          | 10        | $101,000/10 = 10,100$ |

## Median

|          |
|----------|
| \$4,000  |
| \$4,000  |
| \$7,000  |
| \$7,000  |
| \$7,000  |
| \$8,000  |
| \$8,000  |
| \$15,000 |
| \$16,000 |
| \$25,000 |

Order #'s low to high

If odd #: choose middle number

If even #: average two in middle

***Interpretation:*** Half of the people earn more than \$7,500, half earn less.

## Mode

|          |
|----------|
| \$4,000  |
| \$4,000  |
| \$7,000  |
| \$7,000  |
| \$7,000  |
| \$8,000  |
| \$8,000  |
| \$15,000 |
| \$16,000 |
| \$25,000 |

Number that  
occurs most  
frequently =

**\$7,000**

## Arithmetic mean: grouped data

| Income of Households, 2004 (in 1,000's) |          |  |
|---|----------|--|
| <u>Household \$</u>                     | <u>f</u> |  |
| < \$10,000                              | 9,805    |  |
| \$10,000-19,999                         | 14,754   |  |
| \$20,000-39,999                         | 26,904   |  |
| \$40,000-59,999                         | 19,972   |  |
| \$60,000-79,999                         | 14,535   |  |
| \$80,000-99,999                         | 9,362    |  |
| \$100,000+                              | 17,813   |  |
|   | 113,145  |  |

Source: U.S. Census Bureau, Current Population Survey, 2005 Annual Social and Economic Supplement.

## Arithmetic mean: grouped data

| Income of Households, 2004 (in 1,000's) |          |                 |
|---|----------|-----------------|
| <u>Household \$</u>                     | <u>f</u> | <u>Midpoint</u> |
| < \$10,000                              | 9,805    | 5,000           |
| \$10,000-19,999                         | 14,754   | 15,000          |
| \$20,000-39,999                         | 26,904   | 30,000          |
| \$40,000-59,999                         | 19,972   | 50,000          |
| \$60,000-79,999                         | 14,535   | 70,000          |
| \$80,000-99,999                         | 9,362    | 90,000          |
| \$100,000+                              | 17,813   | 100,000         |
|   | 113,145  |                 |

## Arithmetic mean: grouped data

$$\bar{Y} = \frac{\sum fY}{n}$$

$$= \$50,531$$

## Median: grouped data

| Income of Households, 2004 (in 1,000's) |          |  |
|---|----------|--|
| <u>Household \$</u>                     | <u>f</u> |  |
| < \$10,000                              | 9,805    |  |
| \$10,000-19,999                         | 14,754   |  |
| \$20,000-39,999                         | 26,904   |  |
| \$40,000-59,999                         | 19,972   |  |
| \$60,000-79,999                         | 14,535   |  |
| \$80,000-99,999                         | 9,362    |  |
| \$100,000+                              | 17,813   |  |
|   | 113,145  |  |

Source: U.S. Census Bureau, Current Population Survey, 2005 Annual Social and Economic Supplement.

## Median: grouped data

| Income of Households, 2004 (in 1,000's) |          |                     |
|---|----------|---------------------|
| <u>Household \$</u>                     | <u>f</u> | <u>Cumulative f</u> |
| < \$10,000                              | 9,805    | 9,805               |
| \$10,000-19,999                         | 14,754   | 24,559              |
| \$20,000-39,999                         | 26,904   | 51,463              |
| \$40,000-59,999                         | 19,972   | 71,435              |
| \$60,000-79,999                         | 14,535   | 85,970              |
| \$80,000-99,999                         | 9,362    | 95,332              |
| \$100,000+                              | 17,813   | 113,145             |
|   | 113,145  |                     |

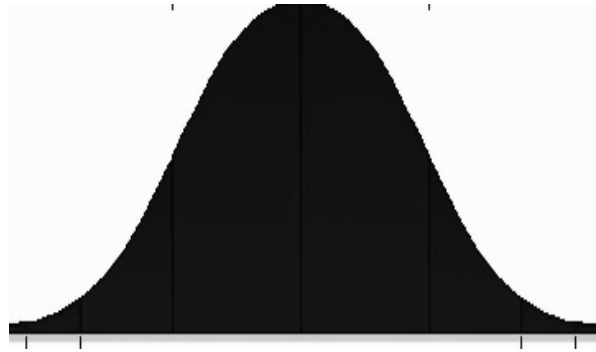
## Median (and percentiles): grouped data

- $113,145 \times .25 = 28286.25$
- $113,145 \times .50 = 56572.5$
- $113,145 \times .75 = 84858.75$

## Mode

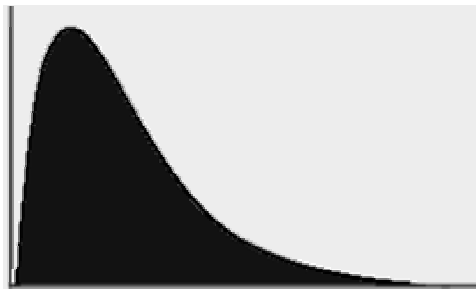
- Can you calculate the mode for this distribution?

## Normal distribution



Mean = Median = Mode

## Positive skew, or skew to the right



Example: income distribution

Negative skew,  
or skew to the left



Example: grade distribution

Bimodal distribution

